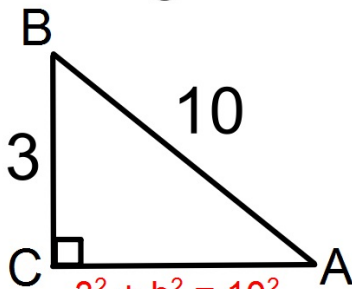


Bellwork

1. Set up the 6 basic trigonometric functions for the given triangle using angle A.



$$\begin{array}{r}
 3^2 + b^2 = 10^2 \\
 9 + b^2 = 100 \\
 \underline{-9 \quad \quad - 9} \\
 b^2 = 91 \\
 b = \sqrt{91}
 \end{array}$$

$$\sin A = \frac{3}{10}$$

$$\csc A = \frac{10}{3}$$

$$\cos A = \frac{\sqrt{91}}{10}$$

$$\sec A = \frac{10 \cdot \sqrt{91}}{\sqrt{91} \cdot \sqrt{91}} = \frac{10 \sqrt{91}}{91}$$

$$\tan A = \frac{3 \cdot \sqrt{91}}{\sqrt{91} \cdot \sqrt{91}} = \frac{3 \sqrt{91}}{91}$$

$$\cot A = \frac{\sqrt{91}}{3}$$

2. How many degrees is the sum of all three angles in a triangle? 180°

Solving Triangles

Given Information Possibilities:

1. The measure of 1 side and 1 angle
2. The measure of 2 sides

Wanted Information:

1. The measure of all 3 sides
2. The measure of all 3 angles

Solving Right Triangles: Given 1 side and 1 angle

Procedure:

1. Find the third angle.

Do so by $90^{\circ} - \text{Given Angle} = ?$

2. Using SOH-CAH-TOA

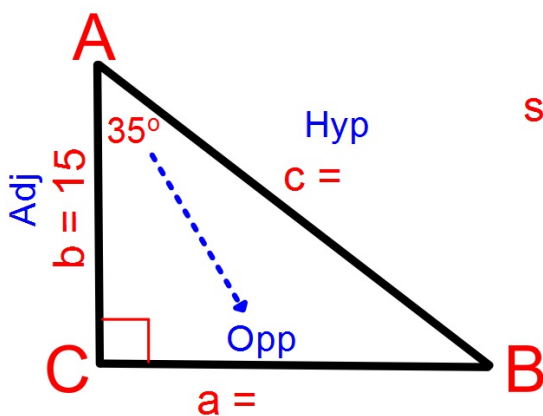
Set up one of these trig functions and solve for the missing side/hypotenuse.

3. Use the Pythagorean Theorem to find the remaining missing side.

Example

Solve the given triangle, round all decimals to the nearest tenth:

1. $\angle A = 35^\circ$ & $b = 15$



Finding the other 2 sides:

Set up SOH-CAH-TOA using $A...$

$$\sin 35^\circ = \frac{a}{c} \quad \cos 35^\circ = \frac{15}{c} \quad \tan 35^\circ = \frac{a}{15}$$

Since \sin contains side a and c we will need to solve the other two for the two missing sides.

$$\frac{c \cdot \cos 35^\circ}{\cos 35^\circ} = \frac{15}{\cos 35^\circ} \quad \& \quad 15 \cdot \tan 35^\circ = a$$

$$c = 18.3$$

$$a = 10.5$$

Finding the third angle:

$$\angle B = 180^\circ - 90^\circ - 35^\circ$$

$$\angle B = 55^\circ$$

Finding Angles Given Only Sides

Inverse Functions:

$\sin^{-1}A$
 $\cos^{-1}A$
 $\tan^{-1}A$ } Will require you to use the 2nd key
and then press sin, cos, or tan

Finding the measure of the angle:

1. Set up the ratio of the sides using
SOH-CAH-TOA

2. Then:

$$\sin^{-1}\left(\frac{\text{Opp}}{\text{Hyp}}\right) = A, \cos^{-1}\left(\frac{\text{Adj}}{\text{Hyp}}\right) = A, \tan^{-1}\left(\frac{\text{Opp}}{\text{Adj}}\right) = A$$

3. Round off to the nearest tenth of a degree

Solving Right Triangles: Given 2 sides

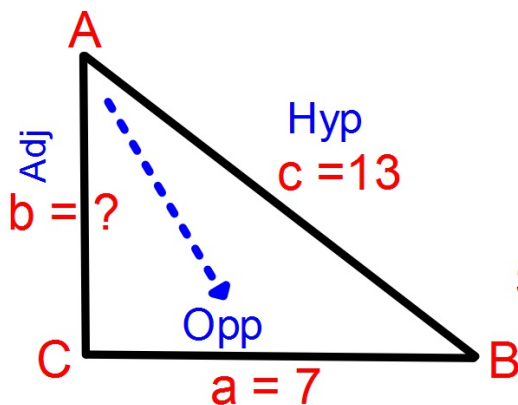
Procedure:

1. Find the third side of the triangle using Pythagorean Theorem.
2. Set up the regular trigonometric functions: SOH-CAH-TOA
3. Find one of the angles using the inverse functions discussed on the previous page.
4. Find the third angle by taking...
 90° - Angle found in step 3
This is because one angle is already 90°

Example

Solve the given triangle, round all decimals to the nearest tenth:

1. $a = 7$ & $c = 13$



Find the third side using Pythagorean Theorem:

$$\begin{aligned}7^2 + b^2 &= 13^2 \\49 + b^2 &= 169 \\-49 &\quad -49 \\ \hline b^2 &= 120 \\ b &= \sqrt{120} \\ b &= \sqrt{4 \cdot 30} \\ \boxed{b} &= 2\sqrt{30}\end{aligned}$$

Select one angle to use, lets say A. We were given a and c, the Opposite and the Hypotenuse. So lets set up sin.

$$\begin{aligned}\sin A &= 7/13 \\ A &= \sin^{-1}(7/13)\end{aligned}$$

$$\boxed{\angle A \approx 32.6}$$

Finally, $\boxed{\angle B = 180^\circ - 90^\circ - 32.6^\circ = 57.4^\circ}$