

Bellwork

Factor each of the following completely:

1. $x^2 + 24x + 144$

2. $x^2 - 28x + 196$

$$\sqrt{x^2} = x$$

$$\sqrt{144} = 12$$

Check: $2(x)(12) =$ middle term

$$x^2 = x$$

$$196 = 14$$

Check: $2(x)(14) =$ middle term

$$\begin{aligned} &(x + 12)(x + 12) \\ &\text{OR} \\ &(x + 12)^2 \end{aligned}$$

$$\begin{aligned} &(x - 14)(x - 14) \\ &\text{OR} \\ &(x - 14)^2 \end{aligned}$$

3. What is the relationship between the coefficient of the middle term and the constant? The relationship is that the middle term is twice the square root of the constant.

Completing the Square

What is completing the square?

Completing the square is a process that allows you to put a quadratic equation in the form $(#x + p)^2$.

Helpful when:

1. Factoring quadratics
2. Graphing quadratics (Next!)
3. Solving quadratics (Coming soon!)

Procedure

Step 1: Divide the middle coefficient by 2.

Step 2: Square the result from Step 1.

Step 3: Write the answer.

Step 4: For practice, you can factor each of the problems out.

Examples

Complete the square:

1. $x^2 + 14x + \underline{\hspace{2cm}}$

$$\left(\frac{14}{2}\right)^2 = (7)^2 = \boxed{49}$$

Factored out:
 $(x + 7)^2$

2. $x^2 - 6x + \underline{\hspace{2cm}}$

$$\left(\frac{-6}{2}\right)^2 = (-3)^2 = \boxed{9}$$

Factored out:
 $(x - 3)^2$

3. $x^2 - 9x + \underline{\hspace{2cm}}$

$$\left(\frac{-9}{2}\right)^2 = \boxed{\frac{81}{4}}$$

Factored out:
 $\left(x - \frac{9}{2}\right)^2$

4. $x^2 + 5x + \underline{\hspace{2cm}}$

$$\left(\frac{5}{2}\right)^2 = \boxed{\frac{25}{4}}$$

Factored out:
 $\left(x + \frac{5}{2}\right)^2$