

Explicit Formula – Day 3
Unit 6: Representations of Linear Relations

Find the explicit formula.

<p>1. 32, 28, 24, 20, ...</p> $\begin{array}{l} 28 - (32) = -4 \\ 24 - (28) = -4 \\ 20 - (24) = -4 \end{array}$ $\begin{array}{l} a_n = d \cdot n + b \\ 32 = -4(1) + b \\ 32 = -4 + b \\ \hline +4 \quad +4 \\ 36 = b \end{array}$ <p>$a_n = -4n + 36$</p>	<p>2. -30, 70, 170, 270, ...</p> $\begin{array}{l} 70 - (-30) = 100 \\ 170 - (70) = 100 \\ 270 - (170) = 100 \end{array}$ $\begin{array}{l} a_n = d \cdot n + b \\ -30 = 100(1) + b \\ -30 = 100 + b \\ \hline -100 \quad -100 \\ -130 = b \end{array}$ <p>$a_n = 100n - 130$</p>
<p>3. -36, -44, -52, -60, ...</p> $\begin{array}{l} -44 - (-36) = -8 \\ -52 - (-44) = -8 \\ -60 - (-52) = -8 \end{array}$ $\begin{array}{l} a_n = d \cdot n + b \\ -36 = -8(1) + b \\ -36 = -8 + b \\ \hline +8 \quad +8 \\ -28 = b \end{array}$ <p>$a_n = -8n - 28$</p>	<p>4. -10, 90, 190, 290, ...</p> $\begin{array}{l} 90 - (-10) = 100 \\ 190 - (90) = 100 \\ 290 - (190) = 100 \end{array}$ $\begin{array}{l} a_n = d \cdot n + b \\ -10 = 100(1) + b \\ -10 = 100 + b \\ \hline -100 \quad -100 \\ -110 = b \end{array}$ <p>$a_n = 100n - 110$</p>
<p>5. -14, -6, 2, 10, ...</p> $\begin{array}{l} -6 - (-14) = 8 \\ 2 - (-6) = 8 \\ 10 - (2) = 8 \end{array}$ $\begin{array}{l} a_n = d \cdot n + b \\ -14 = 8(1) + b \\ -14 = 8 + b \\ \hline -8 \quad -8 \\ -22 = b \end{array}$ <p>$a_n = 8n - 22$</p>	<p>6. -10, -16, -22, -28, ...</p> $\begin{array}{l} -16 - (-10) = -6 \\ -22 - (-16) = -6 \\ -28 - (-22) = -6 \end{array}$ $\begin{array}{l} a_n = d \cdot n + b \\ -10 = -6(1) + b \\ -10 = -6 + b \\ \hline +6 \quad +6 \\ -4 = b \end{array}$ <p>$a_n = -6n - 4$</p>
<p>7. 0, 30, 60, 90, ...</p> $\begin{array}{l} 30 - (0) = 30 \\ 60 - (30) = 30 \\ 90 - (60) = 30 \end{array}$ $\begin{array}{l} a_n = d \cdot n + b \\ 0 = 30(1) + b \\ 0 = 30 + b \\ \hline -30 \quad -30 \\ -30 = b \end{array}$ <p>$a_n = 30n - 30$</p>	<p>8. 13, 6, -1, -8, ...</p> $\begin{array}{l} 6 - (13) = -7 \\ -1 - (6) = -7 \\ -8 - (-1) = -7 \end{array}$ $\begin{array}{l} a_n = d \cdot n + b \\ 13 = -7(1) + b \\ 13 = -7 + b \\ \hline +7 \quad +7 \\ 20 = b \end{array}$ <p>$a_n = -7n + 20$</p>
<p>9. 17, -83, -183, -283, ...</p> $\begin{array}{l} -83 - (17) = -100 \\ -183 - (-83) = -100 \\ -283 - (-183) = -100 \end{array}$ $\begin{array}{l} a_n = d \cdot n + b \\ 17 = -100(1) + b \\ 17 = -100 + b \\ \hline +100 \quad +100 \\ 117 = b \end{array}$ <p>$a_n = -100n + 117$</p>	<p>10. -4, -14, -24, -34, ...</p> $\begin{array}{l} -14 - (-4) = -10 \\ -24 - (-14) = -10 \\ -34 - (-24) = -10 \end{array}$ $\begin{array}{l} a_n = d \cdot n + b \\ -4 = -10(1) + b \\ -4 = -10 + b \\ \hline +10 \quad +10 \\ 6 = b \end{array}$ <p>$a_n = -10n + 6$</p>

11. -6, -3, 0, 3, ...

$$\begin{aligned} -3 - (-6) &= 3 & a_n &= d \cdot n + b \\ 0 - (-3) &= 3 & -6 &= 3(1) + b \\ 3 - (0) &= 3 & -6 &= 3 + b \\ & & -3 & \quad -3 \\ & & \hline & & -9 &= b \end{aligned}$$

$$a_n = 3n - 9$$

12. 29, 49, 69, 89, ...

$$\begin{aligned} 49 - (29) &= 20 & a_n &= d \cdot n + b \\ 69 - (49) &= 20 & 29 &= 20(1) + b \\ 89 - (69) &= 20 & 29 &= 20 + b \\ & & -20 & \quad -20 \\ & & \hline & & 9 &= b \end{aligned}$$

$$a_n = 20n + 9$$

13. -17, -24, -31, -38, ...

$$\begin{aligned} -24 - (-17) &= -7 & a_n &= d \cdot n + b \\ -31 - (-24) &= -7 & -17 &= -7(1) + b \\ -38 - (-31) &= -7 & -17 &= -7 + b \\ & & +7 & \quad +7 \\ & & \hline & & -10 &= b \end{aligned}$$

$$a_n = -7n - 10$$

14. -26, 4, 34, 64, ...

$$\begin{aligned} 4 - (-26) &= 30 & a_n &= d \cdot n + b \\ 34 - (4) &= 30 & -26 &= 30(1) + b \\ 64 - (34) &= 30 & -26 &= 30 + b \\ & & -30 & \quad -30 \\ & & \hline & & -56 &= b \end{aligned}$$

$$a_n = 30n - 56$$

15. 25, -5, -35, -65, ...

$$\begin{aligned} -5 - (25) &= -30 & a_n &= d \cdot n + b \\ -35 - (-5) &= -30 & 25 &= -30(1) + b \\ -65 - (-35) &= -30 & 25 &= -30 + b \\ & & +30 & \quad +30 \\ & & \hline & & 55 &= b \end{aligned}$$

$$a_n = -30n + 55$$

16. -35, -33, -31, -29, ...

$$\begin{aligned} -33 - (-35) &= 2 & a_n &= d \cdot n + b \\ -31 - (-33) &= 2 & -35 &= 2(1) + b \\ -29 - (-31) &= 2 & -35 &= 2 + b \\ & & -2 & \quad -2 \\ & & \hline & & -37 &= b \end{aligned}$$

$$a_n = 2n - 37$$

17. -39, -46, -53, -60, ...

$$\begin{aligned} -46 - (-39) &= -7 & a_n &= d \cdot n + b \\ -53 - (-46) &= -7 & -39 &= -7(1) + b \\ -60 - (-53) &= -7 & -39 &= -7 + b \\ & & +7 & \quad +7 \\ & & \hline & & -32 &= b \end{aligned}$$

$$a_n = -7n - 32$$

18. 24, 17, 10, 3, ...

$$\begin{aligned} 17 - (24) &= -7 & a_n &= d \cdot n + b \\ 10 - (17) &= -7 & 24 &= -7(1) + b \\ 3 - (10) &= -7 & 24 &= -7 + b \\ & & +7 & \quad +7 \\ & & \hline & & 31 &= b \end{aligned}$$

$$a_n = -7n + 31$$

19. -35, -135, -235, -335, ...

$$\begin{aligned} -135 - (-35) &= -100 & a_n &= d \cdot n + b \\ -235 - (-135) &= -100 & -35 &= -100(1) + b \\ -335 - (-235) &= -100 & -35 &= -100 + b \\ & & +100 & \quad +100 \\ & & \hline & & 65 &= b \end{aligned}$$

$$a_n = -100n + 65$$

20. 8, -12, -32, -52, ...

$$\begin{aligned} -12 - (8) &= -20 & a_n &= d \cdot n + b \\ -32 - (-12) &= -20 & 8 &= -20(1) + b \\ -52 - (-32) &= -20 & 8 &= -20 + b \\ & & +20 & \quad +20 \\ & & \hline & & 28 &= b \end{aligned}$$

$$a_n = -20n + 28$$